

In opencv, `ov_core/src/sim/Simulator.cpp`, there is a function to generate 3D points.
`void Simulator::generate_points`. To understand this function, we need to review the concepts:

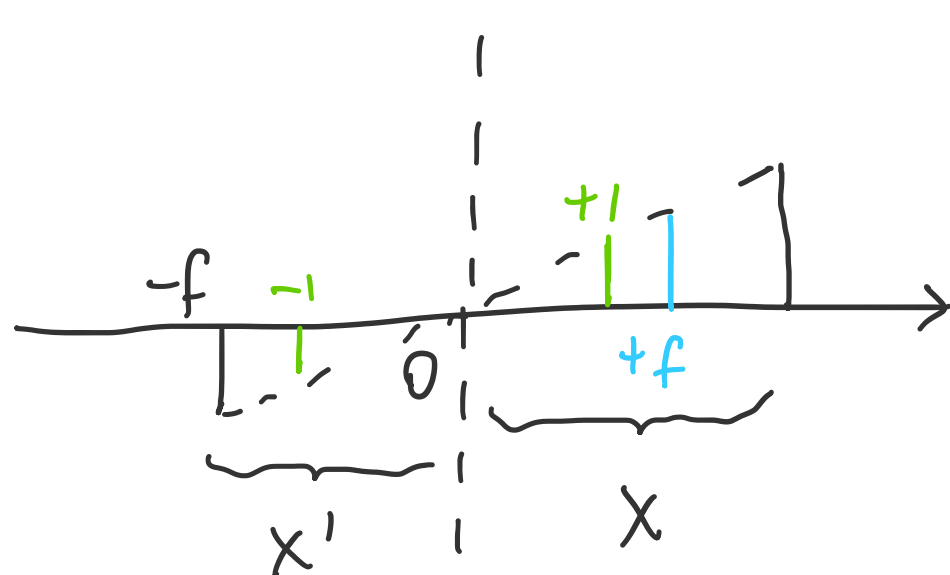
Review: we follow SLAM Book 14 chapters.

For a point $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ in camera frame, the pinhole model

projection is: $\frac{z}{f} = -\frac{x}{x'} = -\frac{y}{y'}$

To simplify, we assume the object is not inverted and get

$$\frac{z}{f} = \frac{x}{x'} = \frac{y}{y'} \Rightarrow x' = f \frac{x}{z} \quad y' = f \frac{y}{z}$$



1: normalized
 1: symmetric projection.
 1: real projection.

from P' , we can get the pixels as:

$$\begin{cases} u = f_x \frac{x}{z} + c_x \\ v = f_y \frac{y}{z} + c_y \end{cases} \Rightarrow \begin{pmatrix} u \\ v \\ 1 \end{pmatrix} = \frac{1}{z} \begin{pmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} \triangleq \frac{1}{z} K P$$

We can rearrange and get

$$z \begin{pmatrix} u \\ v \\ 1 \end{pmatrix} = \begin{pmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} \triangleq K P$$

For a point in world frame P_w :

$$z P_{uv} = z \begin{pmatrix} u \\ v \\ 1 \end{pmatrix} = K (R P_w + t) = K T P_w \Rightarrow P_{uv} = K T P_w$$

Since we are using homogeneous coordinates.

$$\text{For point in camera frame, } P_c = \begin{bmatrix} x \\ y \\ z \end{bmatrix} = (T P_w)_{(1:3)} \Rightarrow \underline{P}_c = \begin{bmatrix} x \\ y \\ z \end{bmatrix} \quad (*)$$

\underline{P}_c can be viewed as a homogeneous coordinate on the $z=1$ plane in front of the camera.

$$P_{uv} = K \underline{P}_c$$

Now come back to the generate points function:

```
for (int i=0; i< numpts; i++) {
```

The numpts is the max. points per frame that we want to see.

```
std::uniform_real_distribution<double> gen_u(0, camera_nh.at(camid).first);
```

This produces random points uniformly sampled from $[0, \text{image width})$.

note that `camera_nh.at(camid)` returns the w, h for camid, and
 .first means the width, .second means height.

```
cv::undistortPoints(mat, mat, camk, camD);
```

This function returns normalized pixels

```
Eigen::Vector3d uv_norm;
```

```
mat = mat.reshape(1);
```

```
uv_norm(0) = mat.at<float>(0,0);
```

```
uv_norm(1) = mat.at<float>(0,1);
```

```
uv_norm(2) = 1
```

uv_norm corresponds to \underline{P}_c in (*)

```
Eigen::Vector3d p_FinC;
```

```
p_FinC = depth * uv_norm;
```

p_FinC is P_c in (*)

```
Eigen::Vector3d p_FinI = R_ItoC.transpose() * (p_FinC - P_IinC);
```

```
Eigen::Vector3d p_FinG = R_GtoI.transpose() * p_FinI + P_IinG;
```

```
p_FinI = R_I^T (p_FinC - P_IinC)
```

```
p_FinG = R_W^T p_FinI + P_IinG;
```

```
featmap.insert({id_map, p_FinG});
```

generate points function returns nothing, the only variable

it changes is featmap, featmap stores the id `id_map` for

each feature position `p_FinG`.

In `Simulator::Simulator(res::NodeHandle & nh)`, which calls

generate points function, we have

```
std::vector<std::pair<size_t, Eigen::VectorXf>> uvs = project_pointcloud(R_GtoI, P_IinG, i, featmap);
```

```
if ((int) uvs.size() < num_pts) {
```

```
    generate_points(R_GtoI, P_IinG, i, featmap, num_pts - (int) uvs.size());
```

```
}
```

This part first projects the points in featmap to the image.

If we are not getting enough observations, then we generate

more points and add them to featmap.