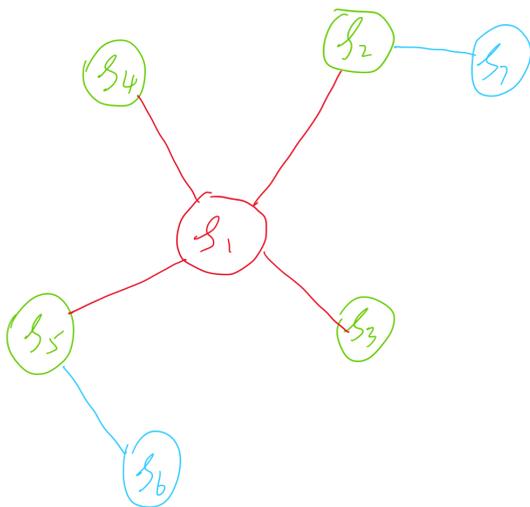
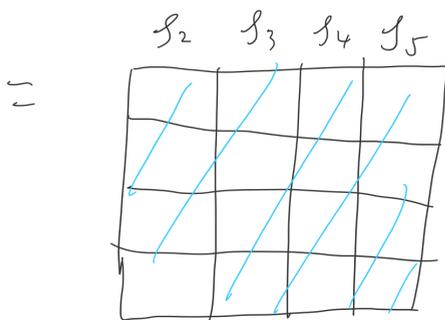
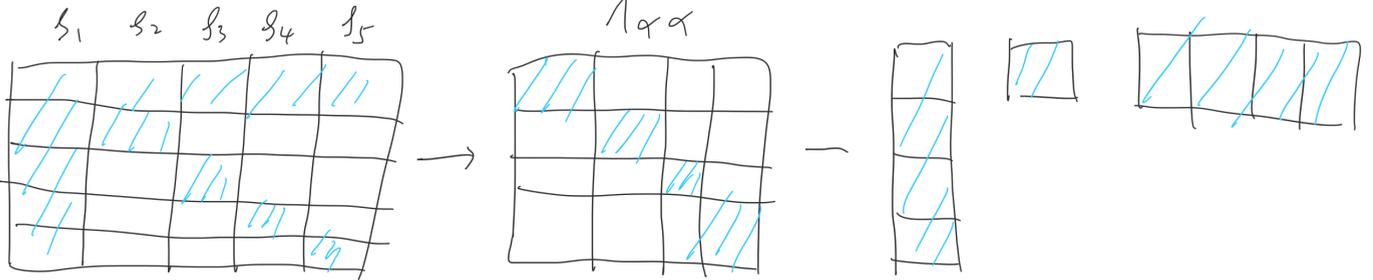


toy eg 3

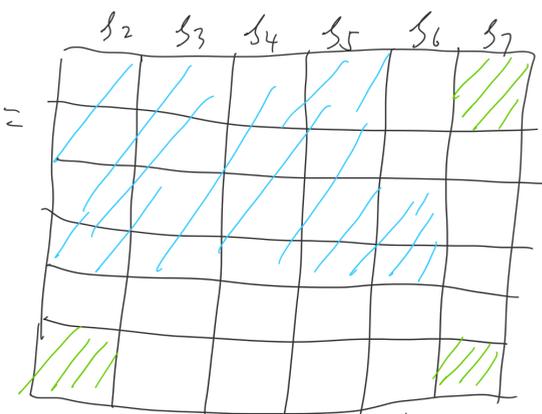
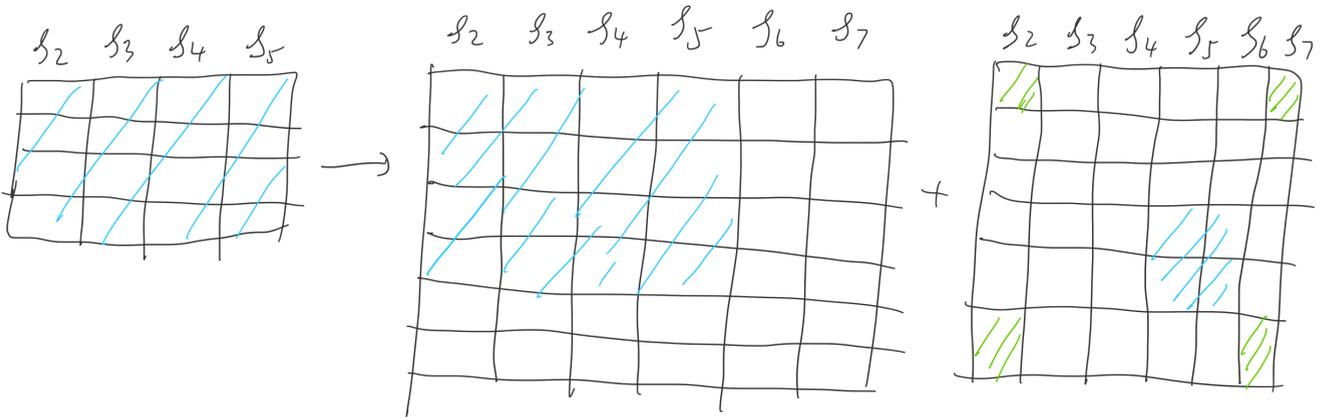


red: Variables and constraints to be marginalized.
 green: variables related to the one to be marginalized
 blue: variables independent to the one to be marginalized.

Step 1: Construct prior



Step 2: prior + new measurements → new info. matrix



Compared with BA, we have added the prior.

issue:

$$\Lambda_p \delta X_p = -b_p$$

when X_p gets updated, how do we change b_p ?

Note that Λ_p is fixed.

If we fix b_p as well, then residuals wrt X_p are not changing, $\therefore X_p$ can't be optimized.

So we have to use Taylor expansion:

$$b_p' = b_p + \frac{\partial b_p}{\partial X_p} \delta X_p$$

$$= b_p + \frac{\partial (-J^T \Sigma^{-1} r)}{\partial X_p} \delta X_p$$

$$= b_p - \Lambda_p \delta X_p$$

$$\frac{\partial (-J^T \Sigma^{-1} r)}{\partial X_p} = -J^T \Sigma^{-1} \frac{\partial r}{\partial X_p}$$

$$= -J^T \Sigma^{-1} J$$

$$= \Lambda_p$$

Sliding window in VINS-mono:

two way marginalization:

1. If the previous image is a key frame, marginalize the oldest frame
2. If the previous image is not a key frame, then discard all visual observations of the previous image, only keep the imu pre-integration.

In VINS-Mono, there's an estimator.cpp:

The most important function is optimization.

```
ceres::Problem problem;
ceres::LossFunction *loss_function; // define problem
...
AddParameterBlock // add vertices
...
MarginalizationFactor // add prior to the problem
...
imu_factor // add imu residual
ProjectionFactor // add reprojection residual.
...
ceres::DOLGLEG // optimize using DOLGLEG.
ceres::Solve
...
double2vector(); // record the state of first pose before and
// after the optimization, and use this transformation
// and apply to all poses in window.
```